

KS3 Mathematics Homework Pack F: Level 8

Stafford Burndred

ISBN 1 84070 031 9



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Meden School and Technology College

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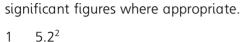
9.....

10.....

11.....

1 Using a calculator (powers, roots and memory)

Use your calculator to find the answers. Show your calculator keys. Give your answer correct to six



6
$$27^{-\frac{1}{4}}$$

7
$$1.6^{-\frac{2}{3}}$$

$$8 \quad \sqrt{2.7^3}$$

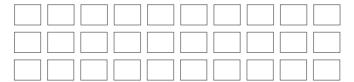
$$9 10^{-3}$$

$$10 (-4)^3$$

11
$$y = 3x^4 + 2x^3 - 6x^2$$

Calculate the value of y when x = 1.29.

Use an efficient calculator method.



12
$$y = 4x^5 - 3x^4 - 2x^3 + 8$$

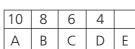
Calculate the value of y when $x = -1.71$.

Use an efficient calculator method.



12.....

Minimum mark 10
Circle grade A



2 Standard form

Write the following numbers in standard form:

- 1 7420 1.....
- 2 538 2......
- 3 0.0732 3.....
- 4
 681.4
 4.......

 5
 0.0006
 5......

Write the following as ordinary numbers:

- 9 3.6 x 10³ 9.....
- 10 7.28 x 10⁵ 10......

- 16 5.43 x 10⁴ 16......

Give the answers to the following:

- a In standard form (correct to three significant figures).
- b As an ordinary number (correct to six significant figures where appropriate). Show your calculator keys for question 17.

- 19 4.852 x 10⁻⁶ x 3.68 x 10⁴ 19a

20b......

Minimum mark 19 16 12 8

Minimum mark 19
Circle grade A

3 Percentages and fractions - 1

- 1 Find $\frac{3}{8}$ of 28
- 2 Find 17% of 80
- 3 Increase 20 by $\frac{3}{16}$
- 4 Increase 24 by 8%
- 5 Increase 6 by 27%
- 6 Decrease 30 by $\frac{2}{5}$
- 7 Decrease 18 by 7%
- 8 Decrease 35 by 76%
- 9 Find $\frac{7}{20}$ of 18
- 10 Increase 23 by 19%
- 11 Decrease 86 by 72%
- 12 Decrease 4.3 by 56%
- 13 Find 18% of 7
- 14 Increase 7.2 by 18%
- 15 Decrease 6.8 by 24%
- 16 Increase 0.27 by 72%
- 17 Increase 28.3 by 16%
- 18 Find 6% of 23
- 19 Decrease 5.07 by 7%
- 20 Increase 6.32 by 8%

1	
---	--

2.													

3.....

4	 	

Minimum mark 1
Circle grade

16	13	10	7	
Α	В	C	D	Ε

4 Percentages and fractions – 2

The normal price of a car is £18 000. In a sale the price is reduced by 8%. What is the sale price of the car?

1 £

An estate agent receives a $2\frac{1}{2}$ % commission on the sale of a house. If the house sells for £64 000, how much commission will she receive?

2 £

A box of Christmas cards is sold for £2.80. $\frac{3}{8}$ of the selling price is given to charity. How much is given to charity?

3 £

The bill for a car repair is £28.40. The garage offers a 15% discount if the bill is paid immediately. Mr Evans pays immediately. How much does he pay?

4 f

Mr Green earned £220 a week. Calculate his new wage if he receives a pay rise of:

5a £

2.5%

3%

5b £

11% C

C

5c £.....

In a sale the following items are reduced by 12%. Calculate the sale prices:

6a £

Shirt, normal price £18

6b f

h Trousers, normal price £22 Hat, normal price £7

6c £.....

Dress, normal price £16.50

6d £

Scarf, normal price £8.50 е

6e f.....

Minimum mark Circle grade

10	8	6	4	
Α	В	\cup	D	Е

5 Percentages and fractions - 3

1 The price of a meal including a 15% service charge was £9.66. How much was the price of the meal before the service charge was added?

1 £

The price of a car including 17.5% VAT was £20 445. What was the price before the VAT was added?

2 f

A dress was reduced in price by 30% in a sale.

The sale price was £18.90. What was the original price?

3 f

4 A man received a wage increase of 7%. His wage after the increase was £398.04. What was his wage before the increase?

4 f

5 A TV cost £493.50 including 17.5% VAT. How much was the VAT?

5 f

6 A picture was sold by a dealer for £728. He made a profit of 12%. How much profit did he make?

6 f

7 Mrs Walker sold a table for £100. She made a loss of $\frac{1}{5}$ by selling at this price. How much money did she lose?

7 £

8 The price of a car increased by 5%. The new price of the car was £21 000. What was the price of the car before the increase?

8 f

Minimum mark Circle grade

7	5	4	2	
А	В	\cup	D	Е

6 Percentages and fractions - 4

1	A woman earns £30 000 per annum. She receives a 4% increase each year. What is her annual salary in three years?	1 £
2	A man earns £500 per week. He receives a 6% increase each year. What is his weekly wage in three years? Give your answer to the nearest penny.	2 f
3	The population of a country is rising by 3% per annum. In 1996 the population was 8 400 000. What was the population in:	
	a 1998?	3a
	b 1999? Give your answer to the nearest whole number.	3b
4	The value of a car decreased by 8% each year. The value in 1998 was £12 000.	
	a What was the value in 1999?	4a £
	b What will be the value in 2001? Give your answer to the nearest penny.	4b f
5	A man's salary increased by 2.5% per annum. In 1992 he earned £15 000. How much did he earn in 1995? Give your answer to the nearest penny.	5 f

Minimum mark Circle grade

7	5	4	2	
Α	В	\cup	Д	Е

8

6 f

A man invests £6000 at 7% per annum compound interest. What is the value of his investment after

three years? Give your answer to the nearest penny.

7 Using algebraic formula - 1



In each question write the value of y correct to six significant figures where appropriate, given $a = \frac{3}{5}$, $b = -\frac{5}{6}$, c = 3.872, d = -2.617.

Evaluate the following:

1
$$y = 3a + 4b$$

$$y = a(b - 3c)$$

$$3 \qquad y = \frac{6a - 4b}{a - b}$$

4
$$y = a\sqrt{bd}$$

$$5 \qquad y = \frac{a + b + c}{3d + c}$$

$$6 y = \sqrt{\left(\frac{\alpha - 3b}{c^2}\right)}$$

7
$$y = \sqrt{a} + \sqrt{c}$$

$$8 \qquad y = \frac{\alpha^2 + b^2}{c^2}$$

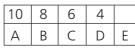
9
$$y = a^3b^2$$

10
$$y = c - 2b(a - b)$$

11
$$y = d - 2b(c + d)$$

12
$$y = d^3 - a^3$$

Minimum mark 10
Circle grade A



8 Using algebraic formula - 2



The volume of a cone is given by the formula $V = \frac{1}{3}\pi r^2 h$. Give all answers correct to three significant figures. Calculate V given:

$$r = 7 \text{ cm}, h = 4 \text{ cm}$$

$$r = 3.5 \text{ cm}, h = 2.8 \text{ cm}$$

Calculate h given:

5
$$V = 27 \text{ cm}^3$$
, $r = 4 \text{ cm}$

6
$$V = 33 \text{ cm}^3, r = 5 \text{ cm}$$

$$V = 32.5 \text{ cm}^3, r = 3 \text{ cm}$$

8
$$V = 17.2 \text{ m}^3$$
, $r = 6.1 \text{ m}$

Calculate r given:

9
$$V = 32 \text{ m}^3$$
, $h = 5.4 \text{ m}$

10
$$V = 84 \text{ m}^3$$
, $h = 7.3 \text{ m}$

11
$$V = 17.2 \text{ cm}^3$$
, $h = 6.2 \text{ cm}$

12
$$V = 23.5 \text{ cm}^3$$
, $h = 5.3 \text{ cm}$

Minimum mark 1 Circle grade

10	8	6	4	
А	В	\cup	D	Е

9 Re-writing formulae - 1

In each question make A the subject:

$$1 \quad B = C + A$$

$$B = C - A$$

$$A = 3C + 2A$$

$$5 C = 3C - 4A$$

$$6 \quad C = ABD$$

$$7 ext{CD} = AB$$

9
$$4CD = 3A + B$$

$$10 5D = 4B - 3AC$$

11 D =
$$\frac{A}{B}$$

12 D =
$$\frac{B}{A}$$

13 C =
$$\frac{AB}{D}$$

$$14 \quad 3C = \frac{BD}{AF}$$

15
$$C = \frac{A}{B} + 3$$

16
$$C = \frac{B}{A} - 2C$$

Minimum mark Circle grade

13	11	8	5	
Α	В	С	D	Е

10 Re-writing formulae - 2

In each question make C the subject:

1
$$\sqrt{C} = A$$

2
$$C^2 = A$$

$$B = \sqrt{(C + A)}$$

$$A = 8C^2$$

$$\sqrt{A} = \sqrt{C}$$

6 A = D +
$$\sqrt{C}$$

$$7 \qquad B = \frac{\sqrt{C}}{AD}$$

$$D = AC^2$$

9 AB =
$$(CD)^2$$

10
$$A = B + C^2$$

11
$$A = B - C^2$$

12 BD =
$$A\sqrt{C}$$

13
$$B = A(C + D)$$

14 B =
$$C(A + D)$$

$$15 \quad B = \frac{D}{C + E}$$

$$16 \quad B = \frac{C + D}{F}$$

16	C=		 	 	

Minimum mark Circle grade

13	11	8	5	
Α	В	\cup	О	Ε

11 Equations - 1

Find the value of y in each equation:

$$1 y + 13 = 7$$

$$2 \quad v - 8 = 3$$

$$3 \quad 3v = -12$$

$$4 -2y = -6$$

$$5 -4v = 2$$

$$6 \quad 7y - 6 = 5y - 14$$

$$7 5y - 8 = 9y + 6$$

$$8 \frac{y}{6} = 3$$

$$9 \frac{y}{4} = -6$$

$$10 \frac{3y}{2} = 12$$

11
$$\frac{2y+3}{4} = 5$$

12
$$\frac{4y-2}{5} = 8$$

13
$$\frac{3}{v} = 12$$

$$14 \frac{4}{v} = -8$$

15
$$\frac{3}{2y} = 12$$

16
$$\frac{5}{4y} = -20$$

Minimum mark 13
Circle grade A

13	11	8	5	
Α	В	\cup	D	Е

12 Equations – 2

Find the value of a, correct to three significant figures where appropriate.

1
$$a^2 = 8$$

$$2 \sqrt{a} = 3.21$$

$$a^2 = 4.2$$

$$4 8a^2 = 48$$

$$5 4 = \frac{3}{a^2}$$

$$6 \quad 6 = \frac{\alpha^2}{4}$$

7
$$28 = \sqrt{a}$$

$$8 42 = 3 + \sqrt{a}$$

9
$$4(a + 3) = 18$$

10
$$3(a + 2) = 5(a - 1)$$

11
$$6(a-2)-2(a+3)=8$$

12
$$5(2\alpha - 3) = 6$$

13
$$4(a + 3) - 5(a - 1) = 2$$

14
$$6(a + 3) = 0$$

15
$$\frac{a+2}{4} = 8$$

$$16 \frac{\alpha - 3}{5} = 10$$

Minimum mark 13 11 8 Circle grade A B C

13 Indices (powers) - 1

Simplify:

1
$$a^5 \times a^7$$

2
$$c^3 \times c^4$$

4
$$y^8 \div y^2$$

5
$$y^6 \div y$$

$$(y^4)^5$$

$$7 (\alpha^3)^2$$

8
$$a^6 \times a^{-4}$$

9
$$a^{-3} \times a^{-2}$$

10
$$a^8 \times \frac{1}{a^5}$$

11
$$a^{-3} \div a^{-5}$$

$$12 \quad \frac{\alpha^4}{\alpha^6}$$

13
$$c^3 x c^2 x c$$

$$14 3c^2 + 5c^2$$

15
$$8y^2 - 3y^2$$

$$16 \quad 10a^3 - 4a^3$$

Minimum mark 13
Circle grade A

13	11	8	5	
Α	В	\cup	О	Ε

14 Indices (powers) - 2

Simplify:

1
$$6y^3 \times 2y^4$$

2
$$3a^4 \times 2a$$

$$3 5a^4c^2 \times 3a^3c^2d$$

4
$$10a^8 \div 5a^4$$

5
$$12a^6 \div 4a^4$$

6
$$15a^5c^3 \div 5a^3c^2$$

$$(3a^2)^2$$

$$8 (5y^4)^2$$

$$\frac{6y^3}{2y}$$

$$10 \quad \frac{8y^6}{4y^3}$$

11
$$\frac{15y^8}{10y^{12}}$$

12
$$\frac{20a^3b^2}{10ab}$$

13
$$\frac{15a^4bc^3}{10ab^3}$$

$$14 \quad \frac{16xy^3z^4}{12x^4yz^2}$$

15
$$(2a^2)^3$$

16
$$2(a^2)^3$$

Minimum mark Circle grade

13	11	8	5	
Α	В	\cup	D	Е

15 Expansion of brackets - 1

Expand the following expressions:

1
$$3(2a + 5)$$

$$2 5(4a - 7)$$

$$3 6(a + 4)$$

4
$$a(3a + 5)$$

6
$$2y^2(3y^3+4y)$$

7
$$6c^3(3c^2 + 2c + 1)$$

10
$$(2a^2 - 3a)2$$

11
$$a^2b^3c^4(a^3b - abc^2)$$

12
$$a^6c^3(ac^2d + ac)$$

13
$$3a^2c(2a + 3c)$$

14
$$5ay (4y^2 - 3a)$$

15
$$3a^2cy^3(2ac - 3y)$$

16
$$6y^3z^2(2\alpha y - 3z^3)$$

Minimum mark Circle grade

13	11	8	5	
Α	В	C	D	Е

16 Expansion of brackets - 2

Expand and simplify the following expressions:

1
$$(a + 3) (a + 5)$$

$$2 (y + 4) (y - 3)$$

$$3 (c-2)(c-5)$$

$$4 (a - 8) (a + 5)$$

$$5 (2x + 5y) (3x + 6y)$$

9
$$(4a + 3c) - (2a + 4c)$$

12
$$6a - 3(a - 4)$$

13
$$a^2 - a(3a + y)$$

14
$$(a - c)^2$$

15
$$(2a - 3y)^2$$

16
$$(3a + 4c)^2$$

Minimum mark Circle grade

13	11	8	5	
Α	В	\cup	D	Е

17 Factorisation – 1

Factorise:

$$5 8x^2 - 14x$$

$$6 \quad 3a^2 - 6a$$

$$7 10c^2 - 5c$$

9
$$8a^4 + 7a^3 - 6a^2$$

$$10 \quad 15c^3 - 10c^2$$

11
$$16d^5 - 12d^3$$

12
$$20y^8 - 16y^6 + 12y^5$$

13
$$a^2c^3 - a^2c + a^2d$$

$$14 \quad 6a^3bc - 12a^2b^2 + 18a^3b$$

$$15 12abc^3 + 8a^2bd$$

$$16 \quad 18a^3cd - 12abc^2$$

Minimum mark Circle grade

13	11	8	5	
Α	В	\cup	D	Е

18 Factorisation – 2

Factorise:

1
$$a^2 + 6a + 8$$

$$2 \quad a^2 + 7a + 6$$

$$3 \quad \alpha^2 - 2\alpha - 15$$

$$4 \quad a^2 + 9a + 14$$

$$5 x^2 - 7x + 10$$

$$6 x^2 + 2x - 15$$

$$7 x^2 - 9x + 8$$

$$8 x^2 - 3x - 40$$

$$y^2 - 9y + 20$$

10
$$y^2 + 13y + 42$$

11
$$y^2 - y - 90$$

12
$$a^2 - b^2$$

Minimum mark Circle grade

10	8	6	4	
Α	В	\cup	D	Е

19 Solving quadratic equations by factorisation



Solve the following quadratic equations by factorisation:

1
$$x^2 - 8x + 15 = 0$$

$$2 \quad \alpha^2 - 3\alpha + 2 = 0$$

$$3 \quad y^2 - 7y + 12 = 0$$

$$4 c^2 + 3c - 10 = 0$$

$$5 \quad x^2 + 8x + 15 = 0$$

$$6 y^2 - 2y - 8 = 0$$

$$7 \quad a^2 + 4a + 3 = 0$$

$$8 \quad (x+1)(x-6) = 0$$

Minimum mark Circle grade

13	11	8	5	
Α	В	\cup	О	Ε

20 Inequalities

Solve the following inequalities:

1
$$x^2 > 64$$

$$y^2 < 81$$

$$3 8 \le 4x < 20$$

4
$$13 \le 3x - 2 \le 31$$

$$-8 \le 2x + 2 < -2$$

$$6 -23 < 3y - 5 < 7$$

7 x is an integer. Write down all of the possible values of x. $4 \le 3x - 2 < 13$

8 y is an integer. Write down all of the possible values of y. $-12 \le 5y - 2 < 7$

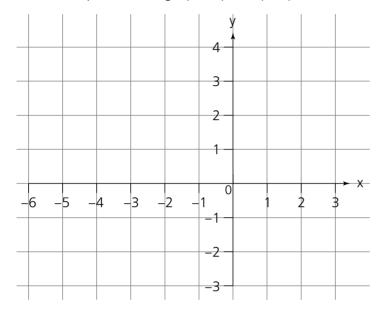
Minimum mark Circle grade

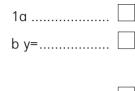
7	5	4	2	
Α	В	\cup	D	Е

21 The straight line equation y = mx + c



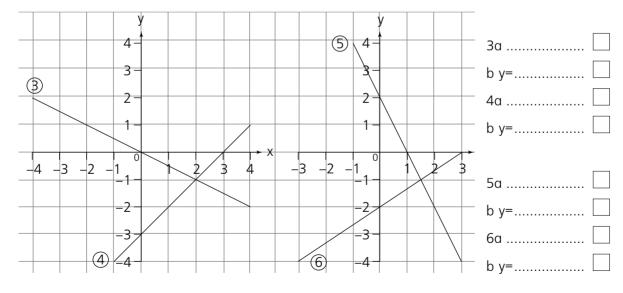
- 1 Find: a The gradient, b The equation of the line which passes through (-1, -3) and (2, 3).
- 2 Find: a The gradient, b The equation of the line which passes through (-6, 4) and (3, 1).







- a What are the gradients of the four lines shown below?
- b What are the equations of the four lines shown below?



Minimum mark 10 8 6 4 Circle grade A B C D E

22 Drawing graphs



Label the following graphs using the **letters** shown below:

$$a y = x$$

$$d v = -x$$

$$q y = x^2$$

$$y = -x^2$$

$$y = x^3 + 1$$

b
$$v = x + 1$$

$$e v = -x + 1$$

h
$$y = x^2 + 1$$

$$k \quad v = -x^2 + 1$$

$$y = -x^3 + 1$$

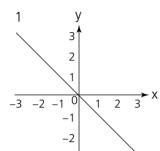
$$v = x - 2$$

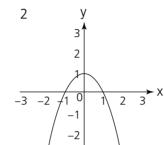
$$f v = -x - 2$$

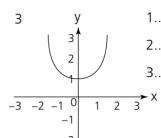
$$v = x^2 - 1$$

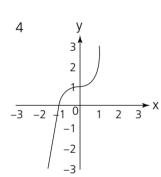
$$v = -x^2 - 1$$

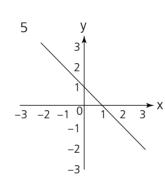
o
$$y = \frac{1}{x}$$

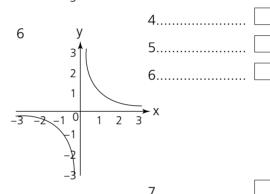


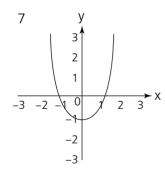


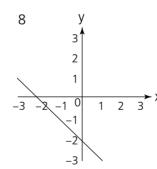


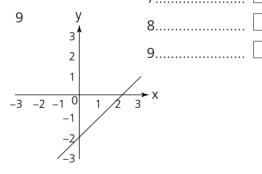


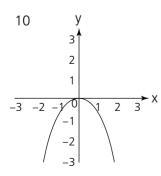


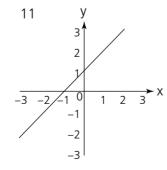


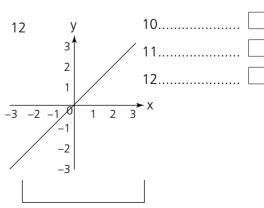












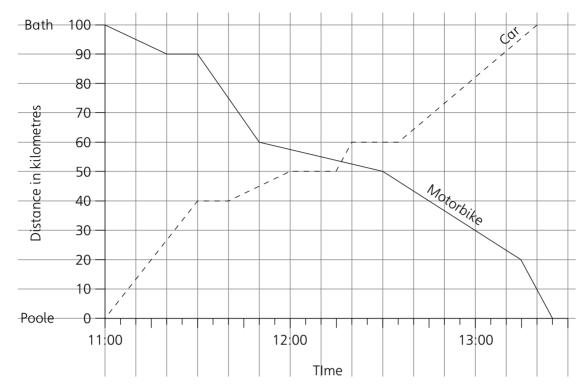
Minimum	mark
Circle gra	de

(10	8	6	4	
	Α	В	C	D	Е

23 Speed, time and distance graphs



This graph shows the journeys made by a car and a motorbike:



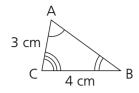
- 1 What time did the car leave Poole?
- 1..... 2 How many times did the car stop? 2.....
- What time did the car arrive in Bath? 3..... 3
- 4..... Between which times did the motorbike travel fastest? 4
- 5 What is the distance from Poole to Bath? 5.....
- How far was the car from Bath at 11:30? 6..... 6
- 7..... What time did the motorbike arrive in Poole? 7
- 8 What time did the car and motorbike pass each other? 8.....
- 9 What was the speed of the motorbike at:
 - 9a 11:15?
- b..... 13:00?
- 10 What was the speed of the car at:
 - 10a 11:15? a b..... b 11:45?

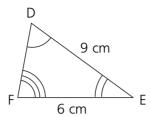
Minimum mark 10 6 Circle grade В

24 Similarity

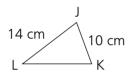


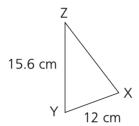
1 Triangle ABC is similar to triangle DEF:





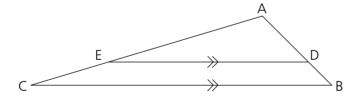
Calculate:





Calculate:

3



DE is parallel to BC.

$$AB = 10 \text{ cm}$$
 $BD = 2 \text{ cm}$

$$AC = 28 \text{ cm}$$
 $BC = 36 \text{ cm}$

Calculate:

Minimum mark Circle grade

7	5	4	2	
Α	В	C	D	Ε

25 Formulae for length, area and volume

a, b, c and d are lengths.

State whether each formula gives a length, area, volume or none of these.

$$1 \quad a + b + c$$

$$2 \quad ab + 3c$$

$$a^2 + bc + 3d$$

$$6 a^2 + bc + cd$$

7 6abc +
$$7b^2c$$

$$8 5a + \frac{cd}{e}$$

9
$$ab^2 + cd^2$$

10 abc +
$$\frac{abc}{d}$$

11
$$a^2b - bc^2$$

$$12 \quad \frac{a^3b}{d} + \frac{abcd}{c} + d^3$$

13
$$\frac{c^3}{d} + a^2 + 2bd$$

$$14 \quad \frac{a^3c}{bd} + \frac{3ab}{c}$$

$$15 \quad \frac{a^3c}{b} \quad - \quad \frac{abcd}{c}$$

$$16 \quad \frac{3abc}{d} + \frac{c^2d}{b}$$

10

Minimum mark 13
Circle grade A

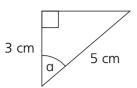
13	11	8	5	
Α	В	\cup	D	Е

26 Trigonometry: Finding an angle

Calculate the size of the angles indicated.

Give your answer correct to three significant figures.

1



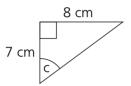
1 a=.....

2



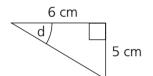
2 b=

3



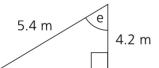
3 c=.....

4



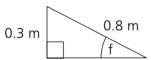
4 d=.....

5



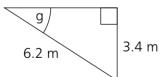
5 e=.....

6



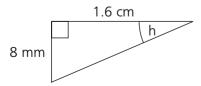
6 f=.....

7



7 g= __

8



8 h= __

Minimum mark
Circle grade

7 5 4 2 A B C D E

27 Trigonometry: Finding a side



Find the size of the sides indicated.

Give your answer correct to three significant figures.

1 6 cm

1.....

2 7 cm 57° b

2.....

3 3.7 m c

3.....

4 10 cm 48° d

4.....

5 4.8 m e

5.....

6 12 cm

7

8

6.....

7.2 m

7.....

5 cm 64° h 26°

8.....

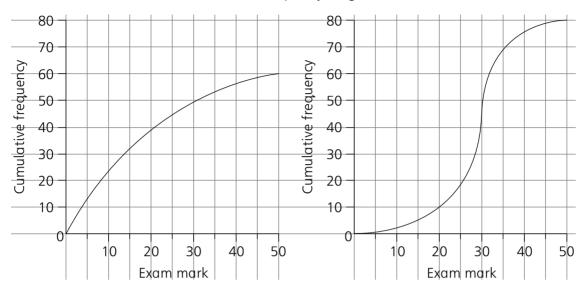
Minimum mark Circle grade

7 5 4 2 A B C D E

28 Using cumulative frequency diagrams to compare distributions

Pupils in two schools each took the same maths exam.

The results are shown in the cumulative frequency diagrams.



- 1 What is the median of:
 - a School A?
 - b School B?
- 2 What is the upper quartile of:
 - a School A?
 - b School B?
- 3 What is the lower quartile of:
 - a School A?
 - b School B?
- 4 What is the interquartile range of:
 - a School A?
 - b School B?
- 5 Use the median and interquartile range to compare School A and School B

Comparison

Minimum mark [

Circle grade

8 6 5 3 A B C D E

10

1a

b

2a

b

3a

b

4a

b

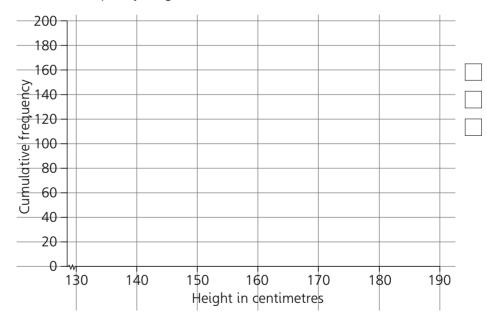
2 marks for comparison

29 Cumulative frequency

This table shows the height of pupils, in centimetres, in a school:

Height in centimetres	Frequency	Cumulative frequency
130 – under 140	8	8
140 – under 150	16	24
150 – under 160	58	
160 – under 170	87	
170 – under 180	28	
180 – under 190	3	

- 1 Complete the cumulative frequency column.
- 2 Complete the cumulative frequency diagram.



Draw relevant lines on the diagram to show how you answered these questions:

3 What is the	median?

3.....

4 What is the upper quartile?

4.....

5 What is the lower quartile?

······

6 What is the interquartile range?

5.....

7 How many pupils were over 175 cm?

7.....

Minimum mark Circle grade

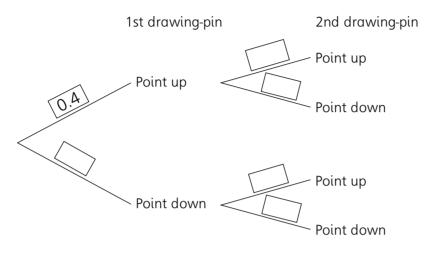
10	8	6	4	
Α	В	\cup	D	Е

30 Probability



1 The probability of a drawing-pin landing point up is 0.4, the probability of landing point down is 0.6. Two drawing-pins are dropped.

Complete the tree diagram to show this:



Use your tree diagram to answer the following questions:

a What is the probability of both drawing-pins landing:

į	Point up?

ii	Point	down?

b	What is the	probability	of at	least	one	drawing	g-
	pin landing	point up?					

- The chance that a battery does not work is 0.02. What is the chance that the battery does work?
- 3 Four coins are tossed. What is the probability of:
 - a Four heads?
 - b Four tails?
 - c At least one head?
 - d At least one tail?

1ai	 	Ш	

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)

2		
L	 	

34	
эu	

Minimum mark Circle grade

7	5	4	2	
Α	В	С	D	Е